

ICCD 2003

Paradigm Shift For Jitter And Noise In Design And Test > 1 Gb/s Communication Systems

**Mike Li and Jan Wilstrup
Wavecrest**



Purposes

- Illustrate the shortfalls of simple parametric based jitter/noise analysis methods (Peak-to-Peak or RMS only)
- Introduce the PDF and CDF based statistical jitter/noise analysis methods
- Introduce the jitter/noise transfer function and its role in serial data link
- Apply both statistical analysis and transfer function for jitter, noise, and BER in modeling and testing > 1 Gb/s systems



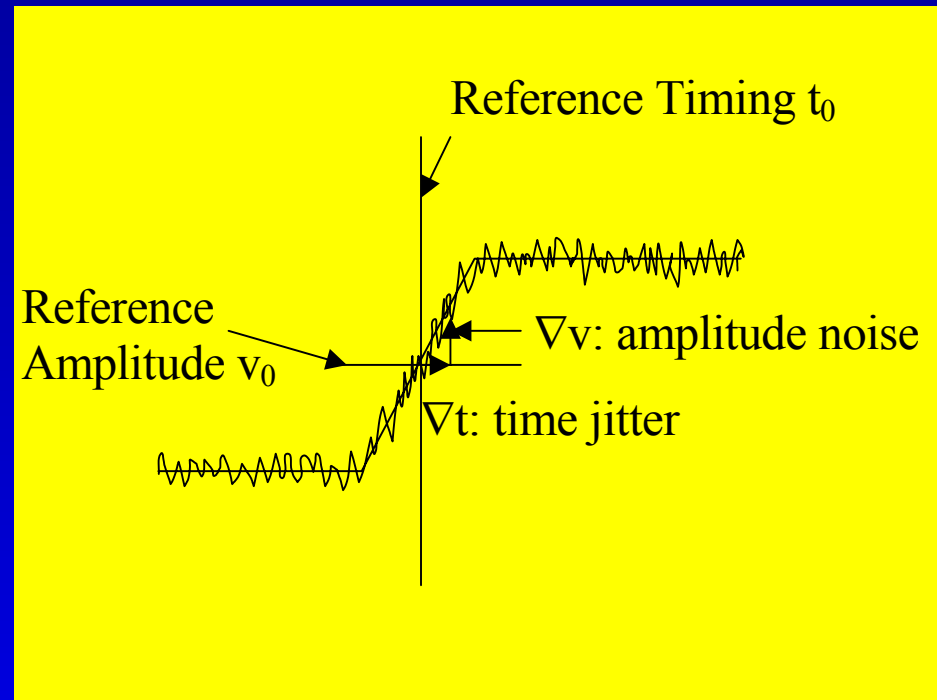
Outline

- Overview of jitter and noise basic
- Shortfalls for parametric peak-to-peak
- PDF and CDF functions jitter, noise, and BER
- Overview of serial communication systems
- Jitter/noise transfer function
- Methods for estimating and testing jitter, noise, and BER
- Conclusion



Jitter And Noise Basics

- Timing Jitter : Any deviation from ideal timing
- Amplitude Noise: Any deviation from ideal amplitude
- Timing jitter occurs when there is an edge transition
- Amplitude noise is a constant activity

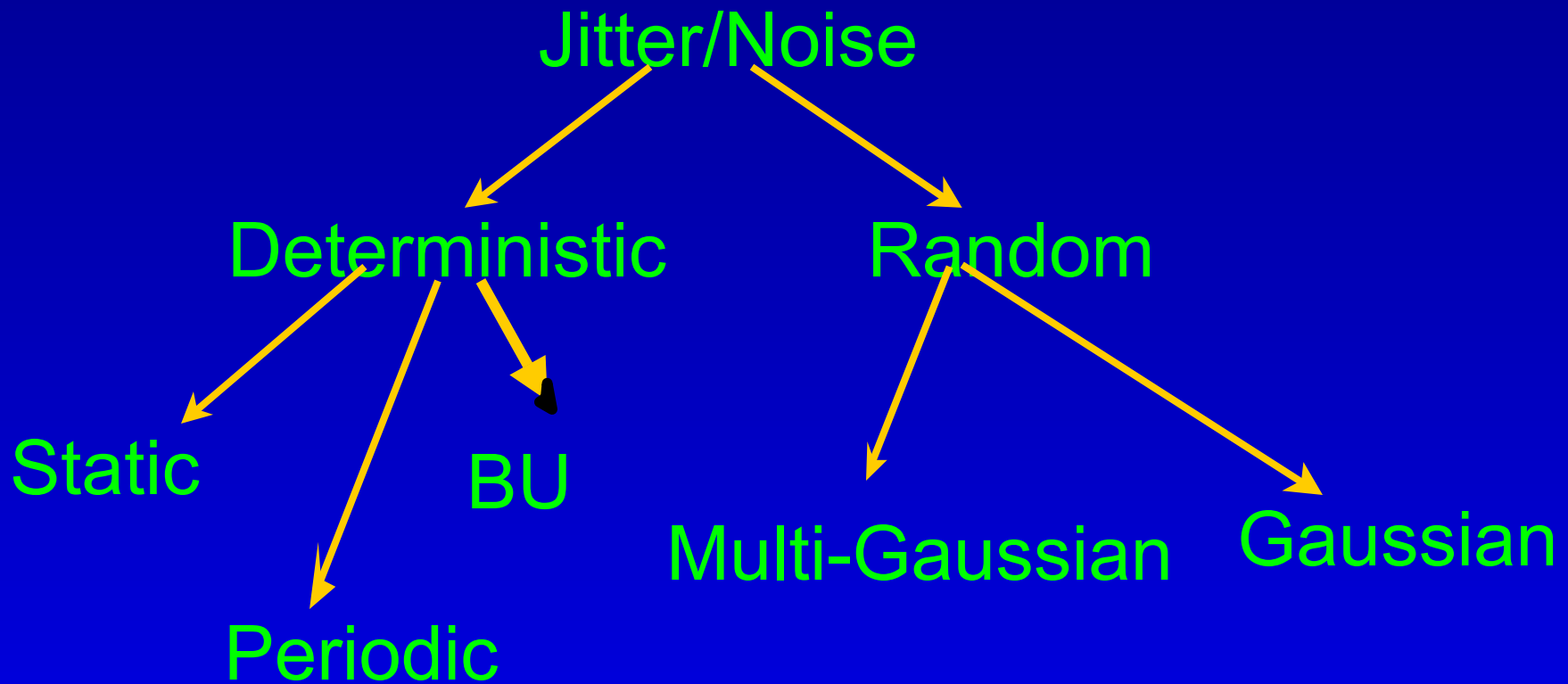


Jitter And Noise Viewed From Signal Theory

- Jitter/noise is a statistical process
- Jitter/noise has a distribution
- Jitter/noise has many different components
- Jitter/noise can only be completely quantified by its PDF !!!



Jitter Classification Scheme (Statistical Based)



BU: Bounded uncorrelated



Relationship Between Total PDF And Component PDFs: *Convolution*

- An example for timing jitter PDF

$$\begin{aligned} p_{TJ}(t) &= p_{RJ}(t) * p_{DJ}(t) \\ &= \int_{-\infty}^{\infty} p_{DJ}(\tau) p_{RJ}(t - \tau) d\tau \end{aligned}$$



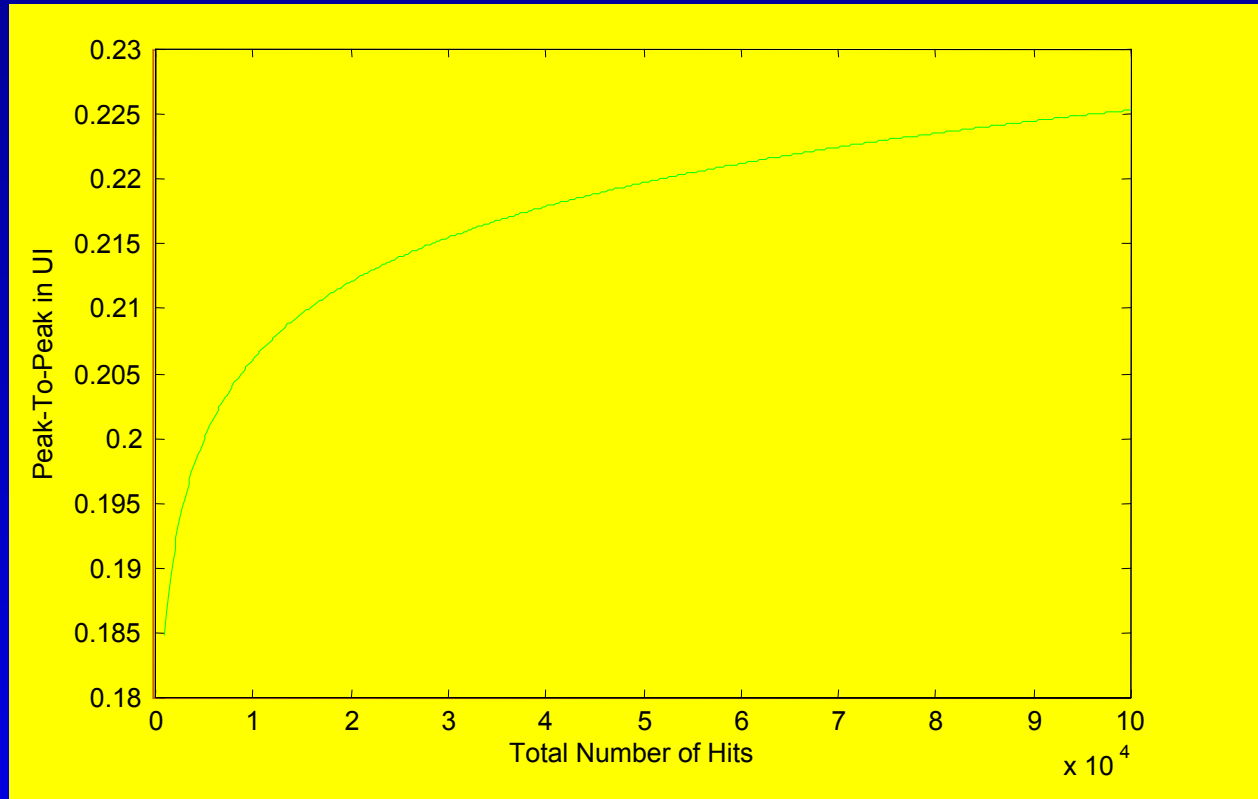
Why *Deterministic* Parametric (i.e, Peak-To-Peak or RMS) No Longer Sufficient?

- Peak-to-peak or RMS alone **cannot** determine a general PDF
- Peak-to-peak will be an **unstable** and size **sample size dependent** estimation in the presence of random component
- RMS will be an **inaccurate** estimation for a Gaussian random in the presence of deterministic component



A Peak-To-Peak Shortfall Case Study

- Sample Size Dependency

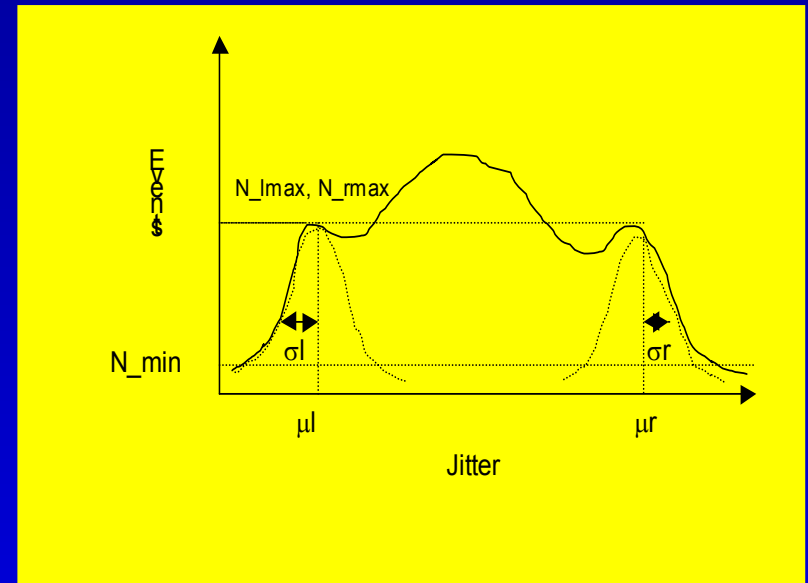


A RMS Shortfall Case Study

RMS \neq RJ sigma

$$RMS = \sqrt{\frac{1}{N-1} \sum_{n=1}^N (\overline{\Delta t} - \Delta t_i)^2}$$

$> \sigma$



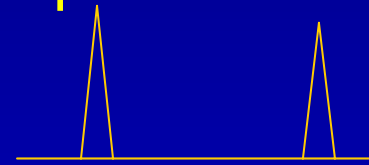
A Deterministic And Random PDF Estimation Method: TailFit (Patented)

- Total jitter PDF = DJ PDF * RJ PDF
- RJ PDF is a Gaussian

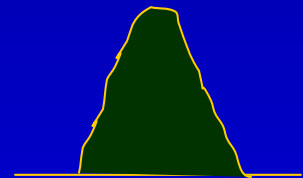
$$p(\Delta t) = \frac{1}{\sqrt{2\pi}} e^{-\frac{(\Delta t - \mu)^2}{2\sigma^2}}$$

- **Tail parts** of distribution preserve information on RJ process.

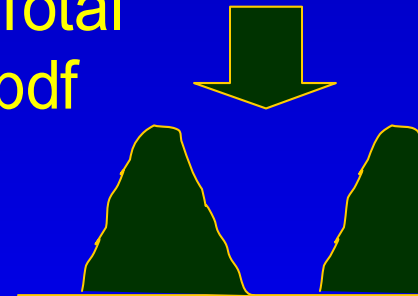
DJ pdf



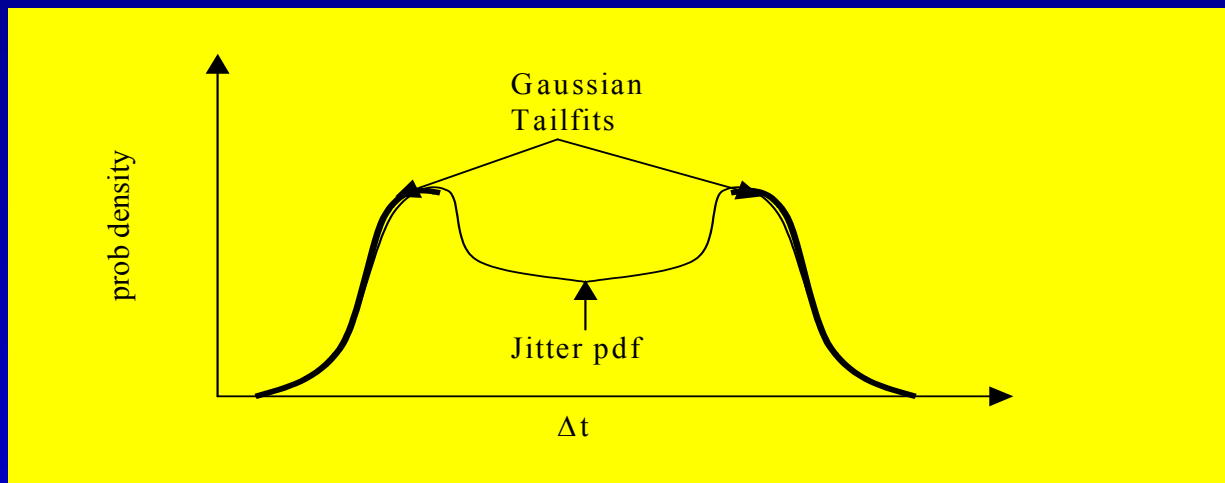
RJ pdf *



Total pdf



What Does The “TailFit” Offer ?

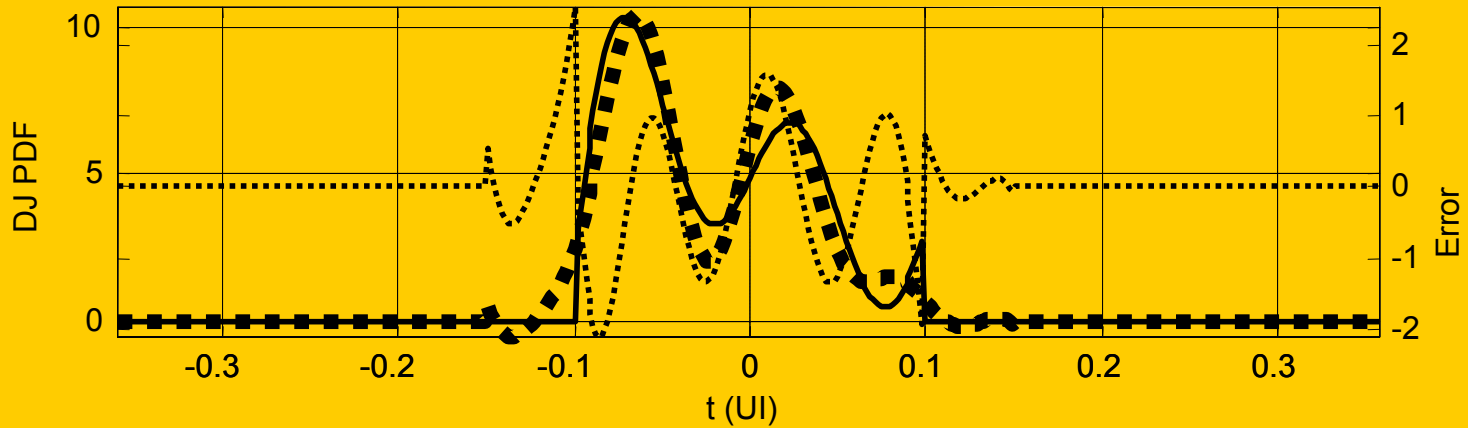
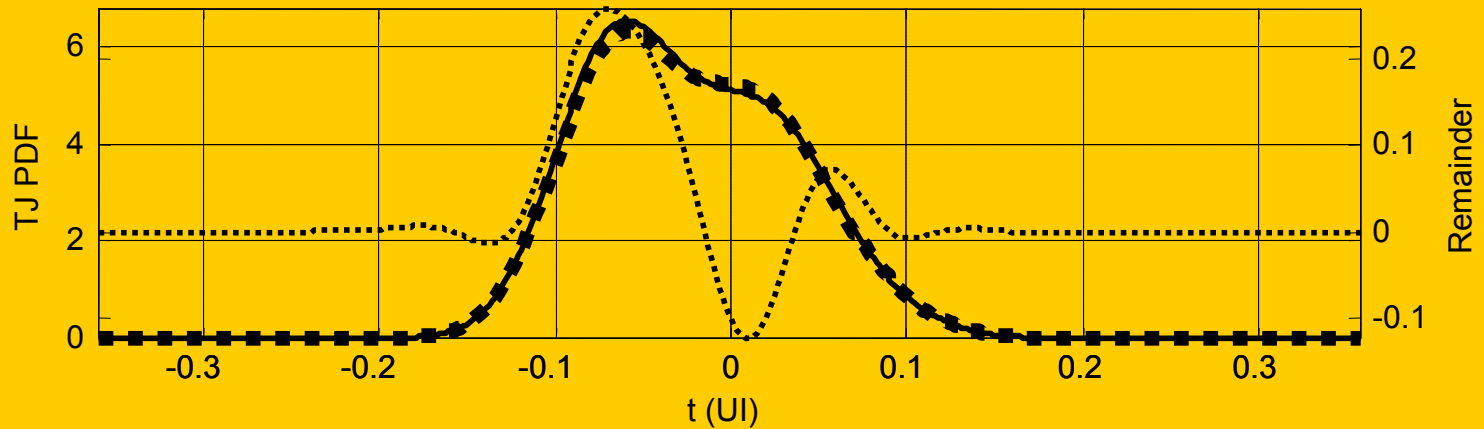


- RJ PDFS
- DJ PDF (via deconvolution)
- Subspace statistical parameters

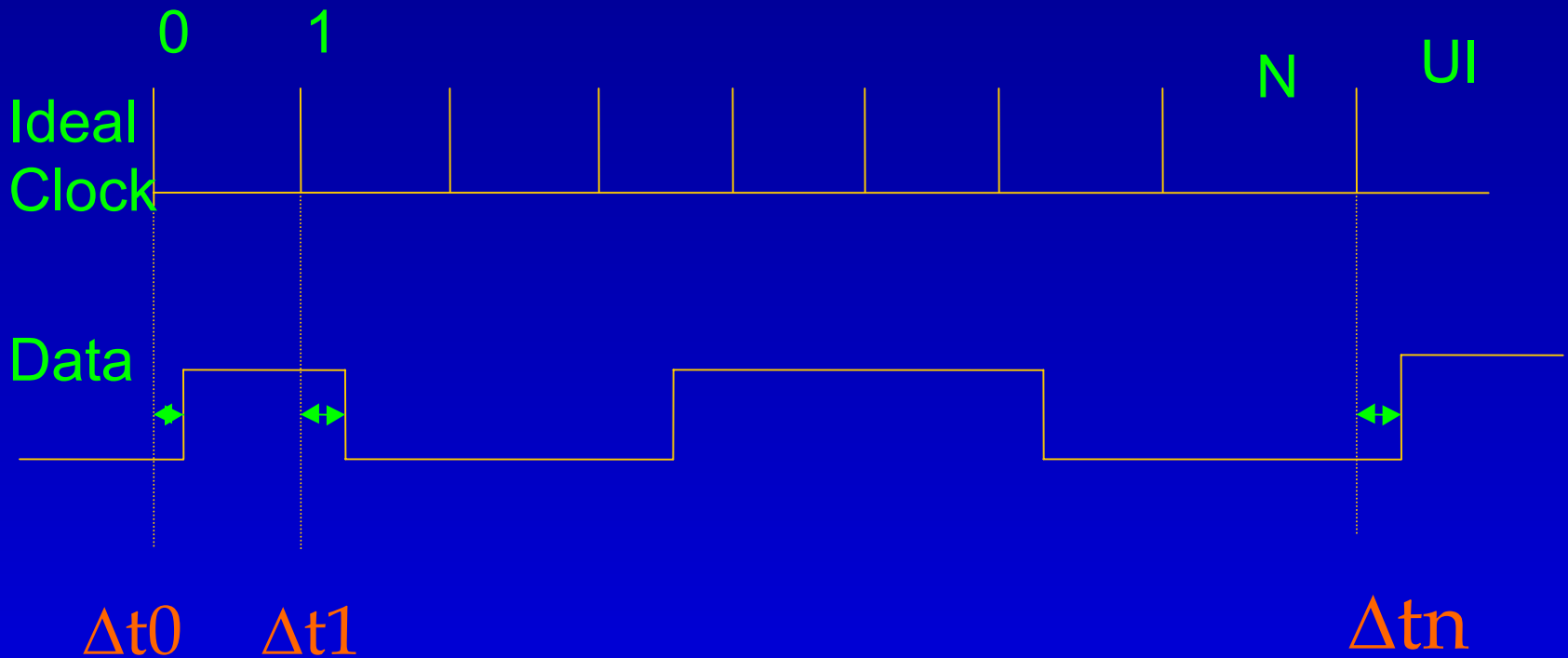


DJ PDF Via Deconvolution

TJ PDF and DJ PDF



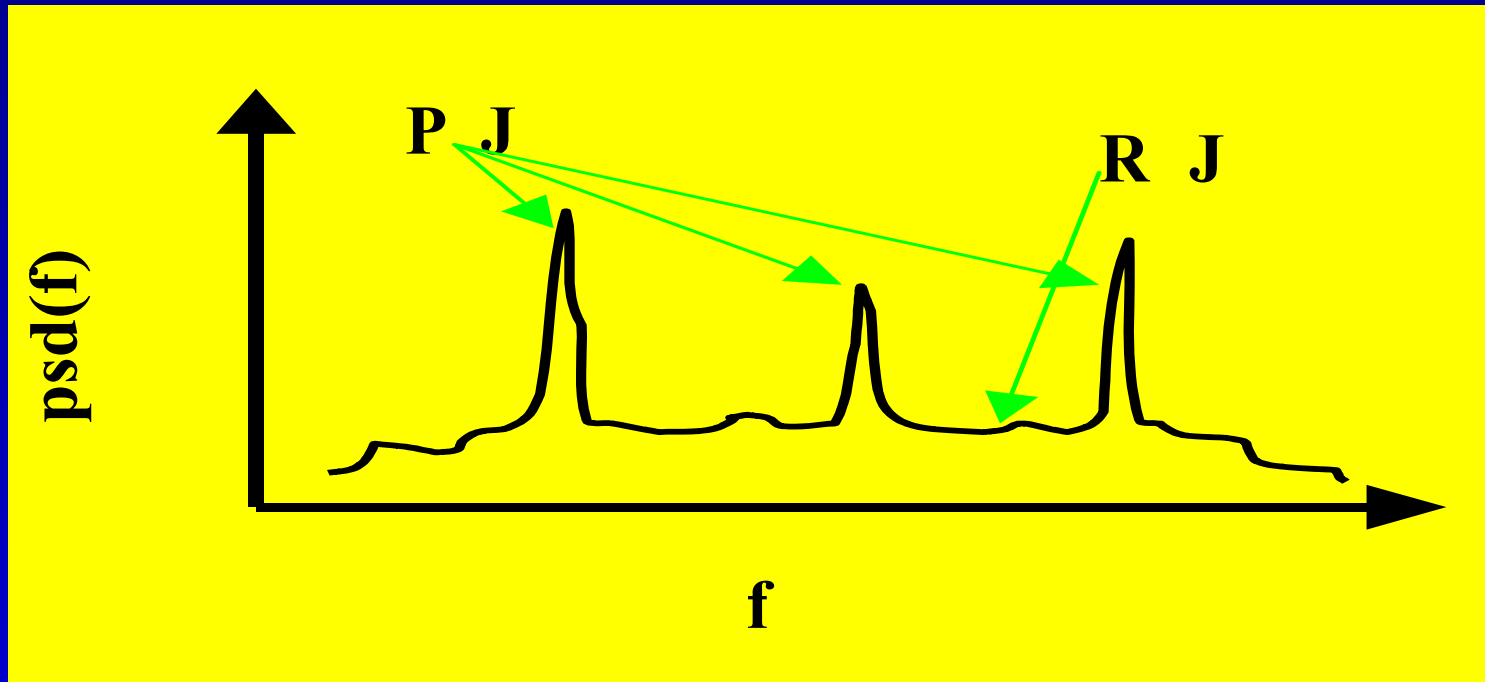
A Jitter/Noise Spectrum Estimation Method: Autocorrelation (Patented)



$$PSD(f) = FFT(c - 2 * R_{xx}(\Delta t(n)))$$



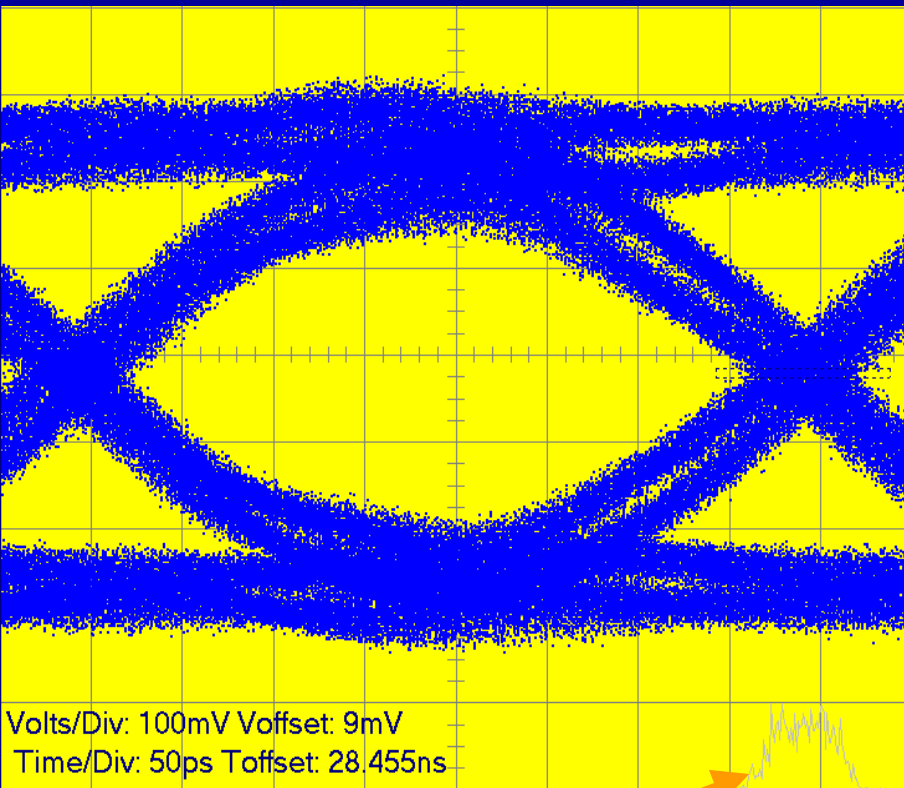
What Does The “Autocorrelation” Offer ?



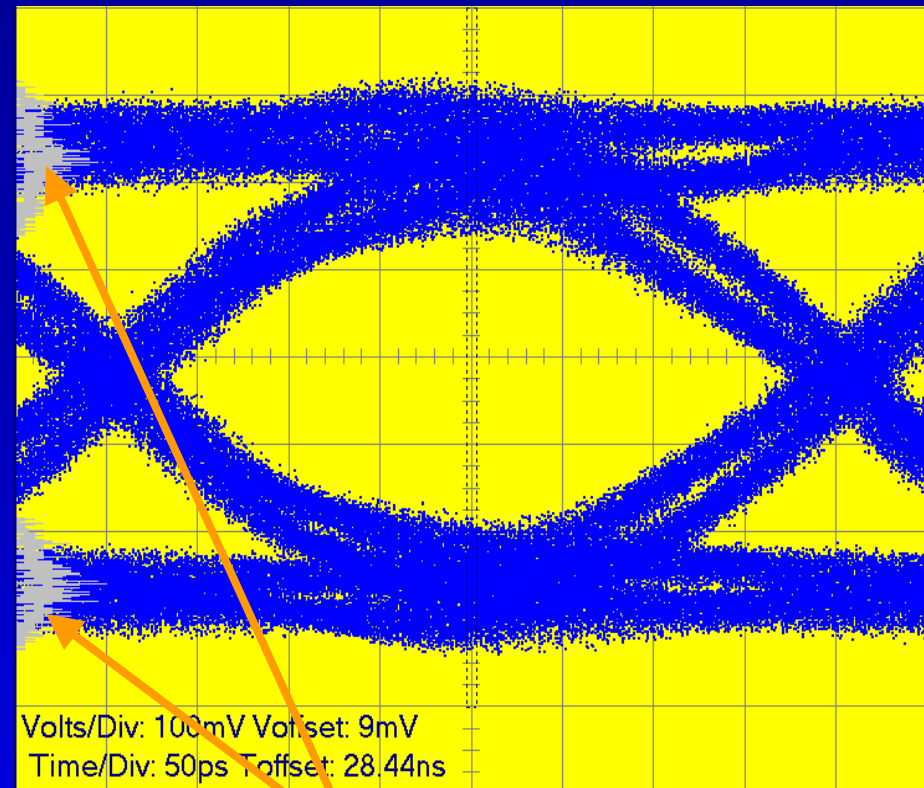
- RJ PSD
- PJ PSD
- DDJ (DJ without PJ and BUJ) PSD



Jitter And Noise In One View: Eye-Diagram



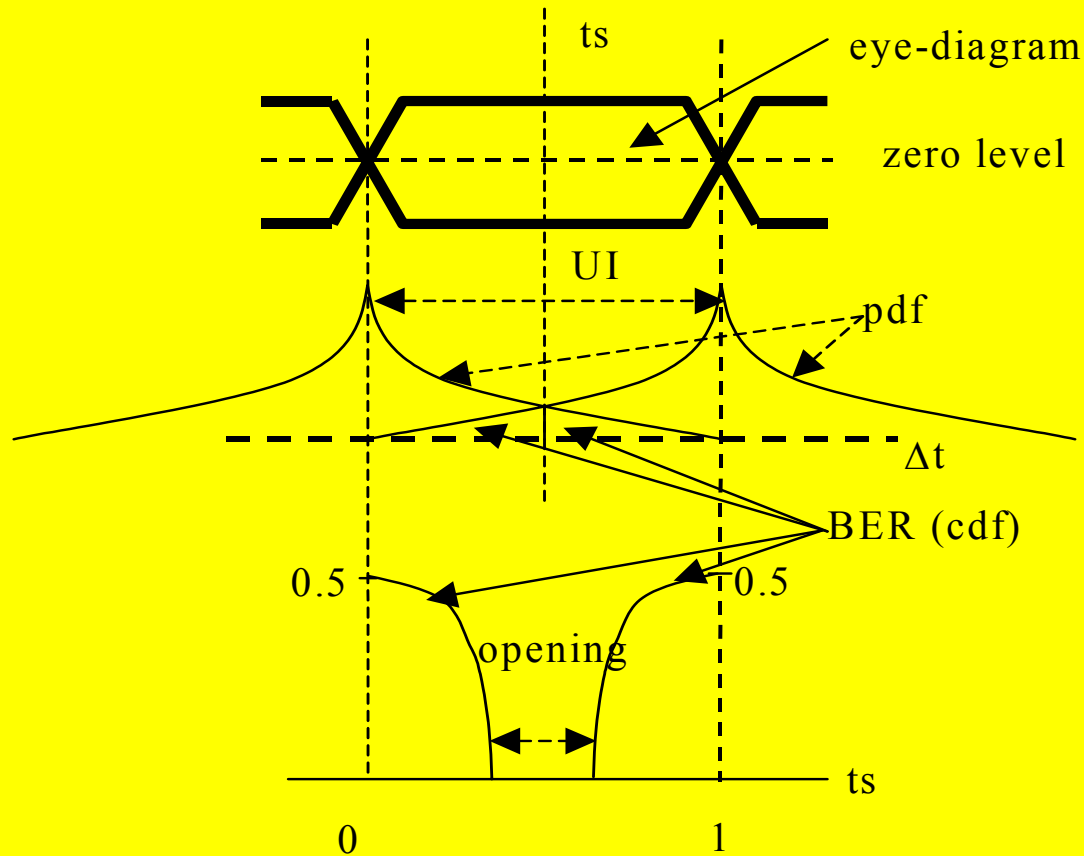
Timing jitter pdf



Amplitude noise pdf



Jitter, Noise, And BER



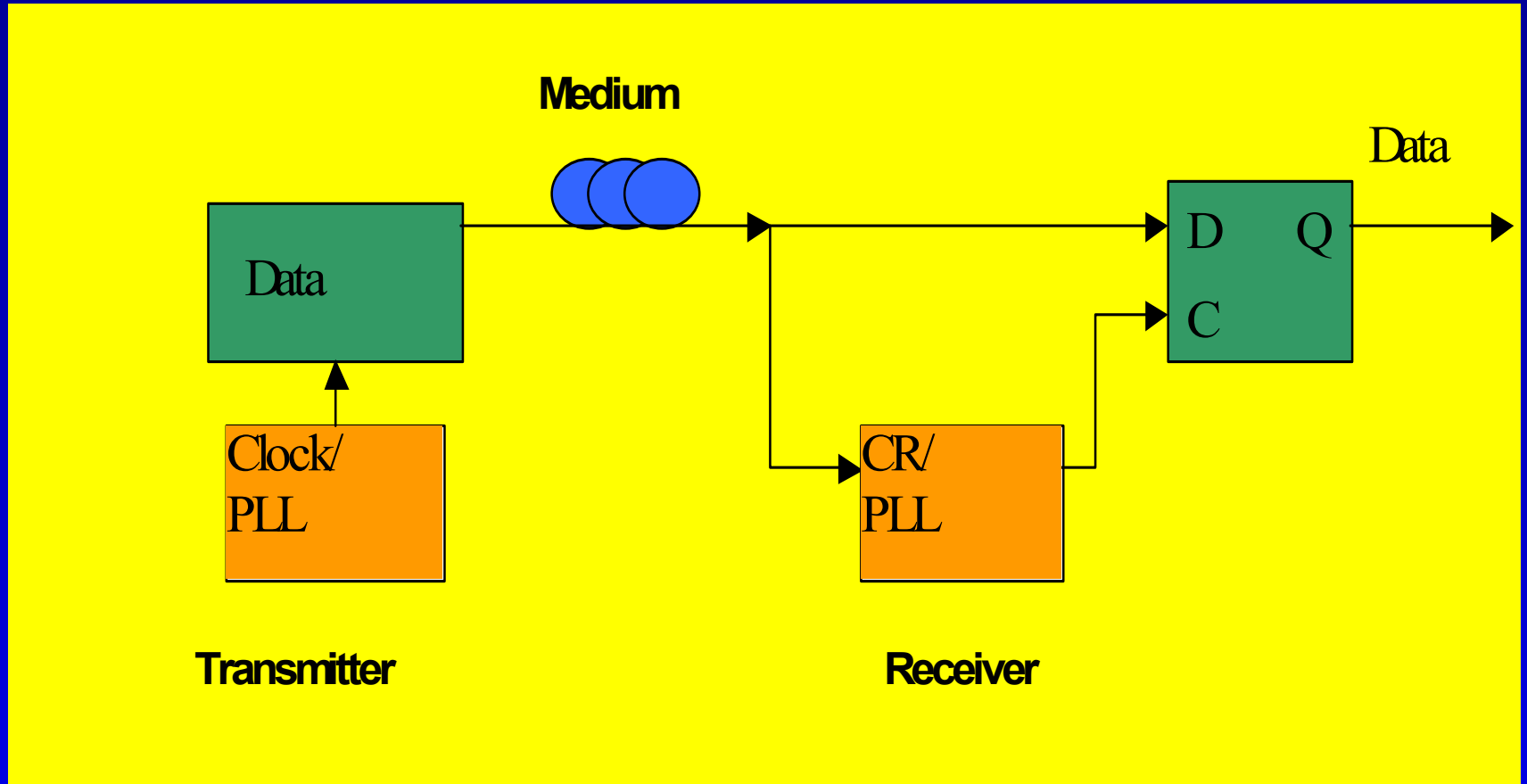
Jitter, Noise, And BER Cont...

- BER: metric for overall system performance
- BER: CDF from jitter and noise PDFS

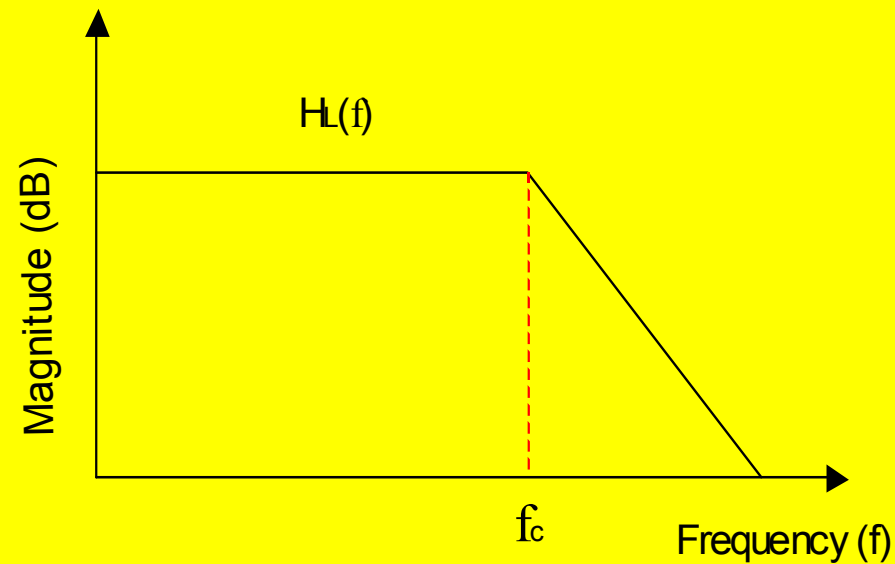
$$BER(t_s) = CDF(t_s) = \frac{1}{2} \left[\int_{t_s}^{\infty} P_{tl}(\Delta t) d(\Delta t) + \int_{-\infty}^{t_s} P_{tr}(\Delta t) d(\Delta t) \right]$$



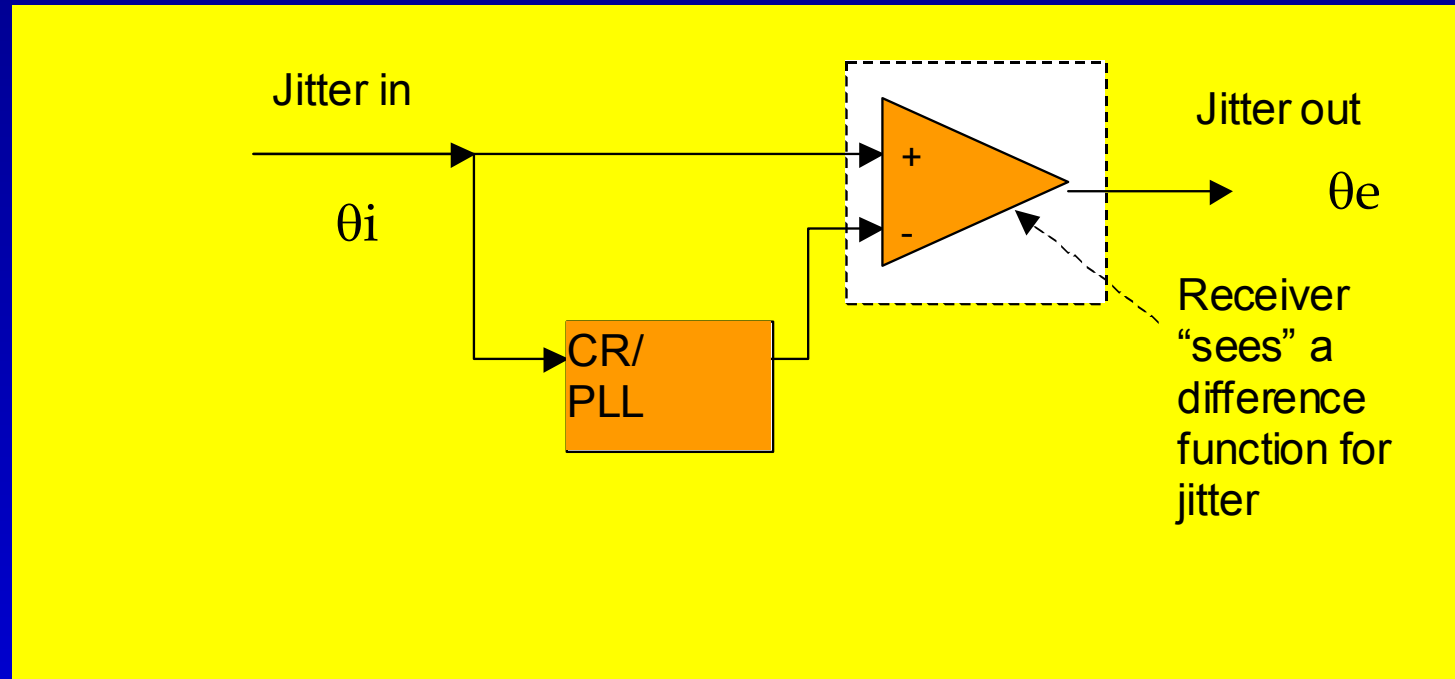
A Serial Data Communication System



A PLL Frequency Response Function



Receiver Jitter Transfer Function



- A “difference” function

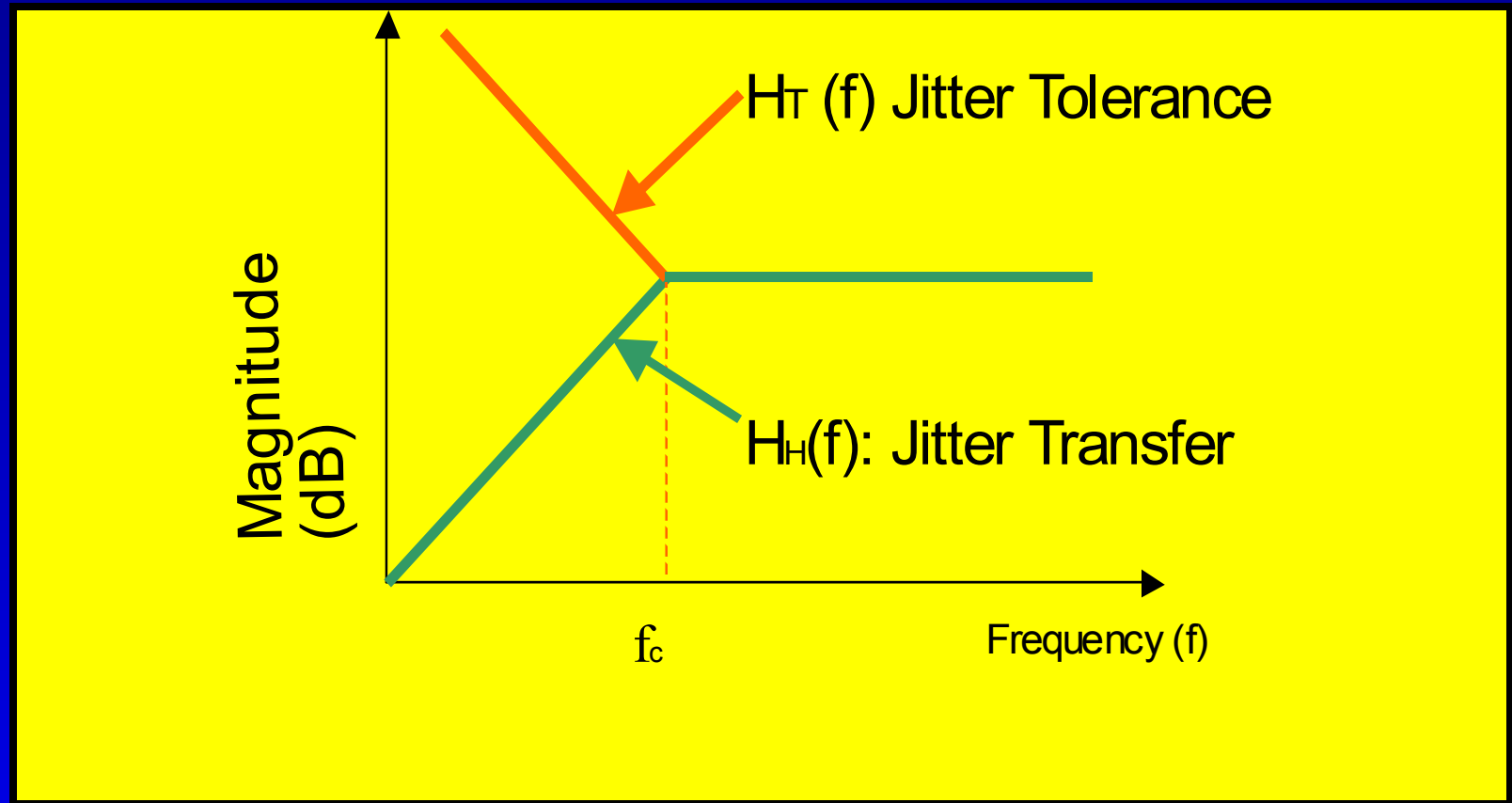


What Does A Difference Function Mean?

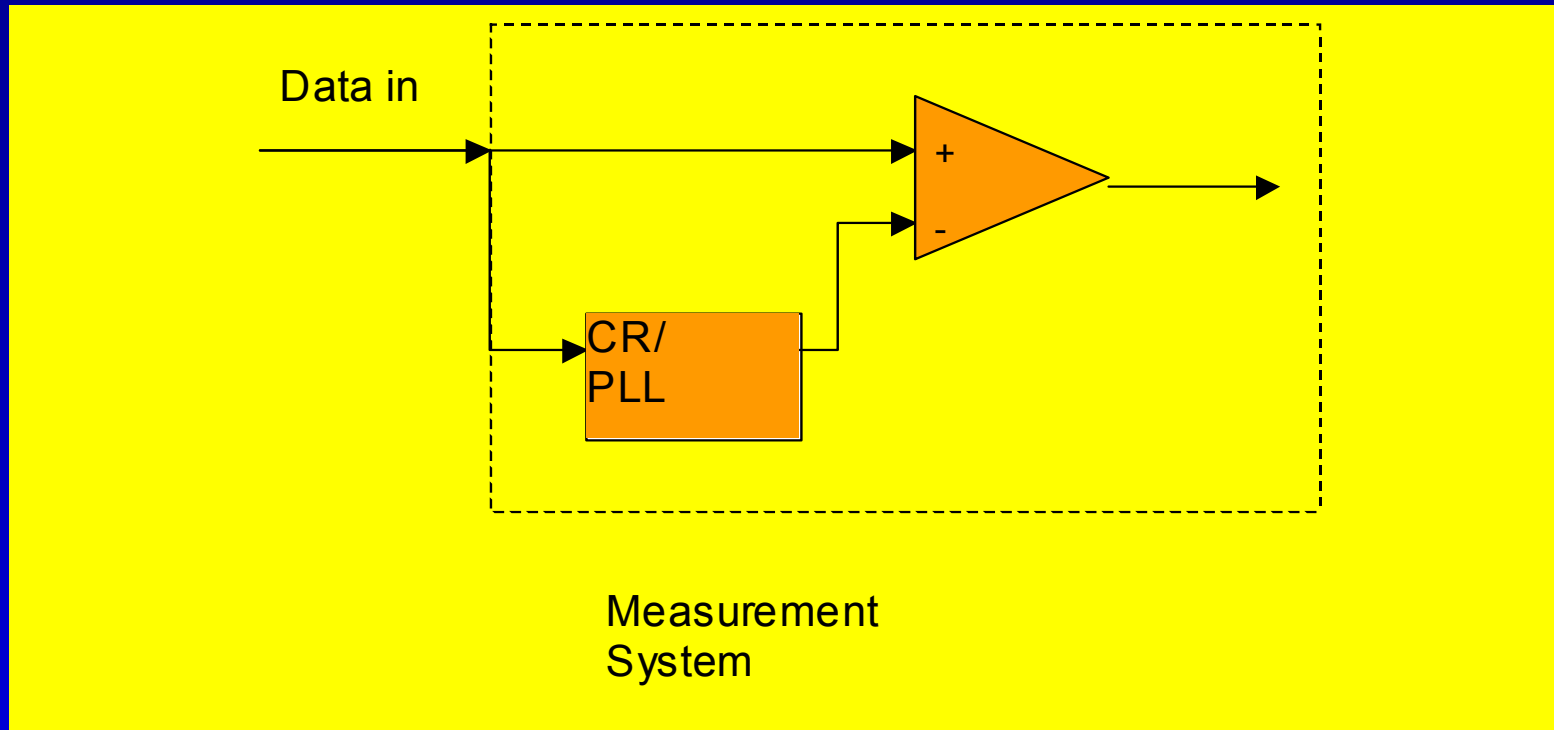
- Jitter is referenced to a recovered bit clock
- Receiver has a jitter transfer function
- “Intrinsic” jitter referenced to an ideal bit clock is not the jitter “seen” by the receiver
- BER of the system should be estimated based on jitter “seen” by the receiver



Jitter Transfer/Tolerance Functions For Data Recovery



What Constitutes A Valid Jitter Estimating/Testing Method?

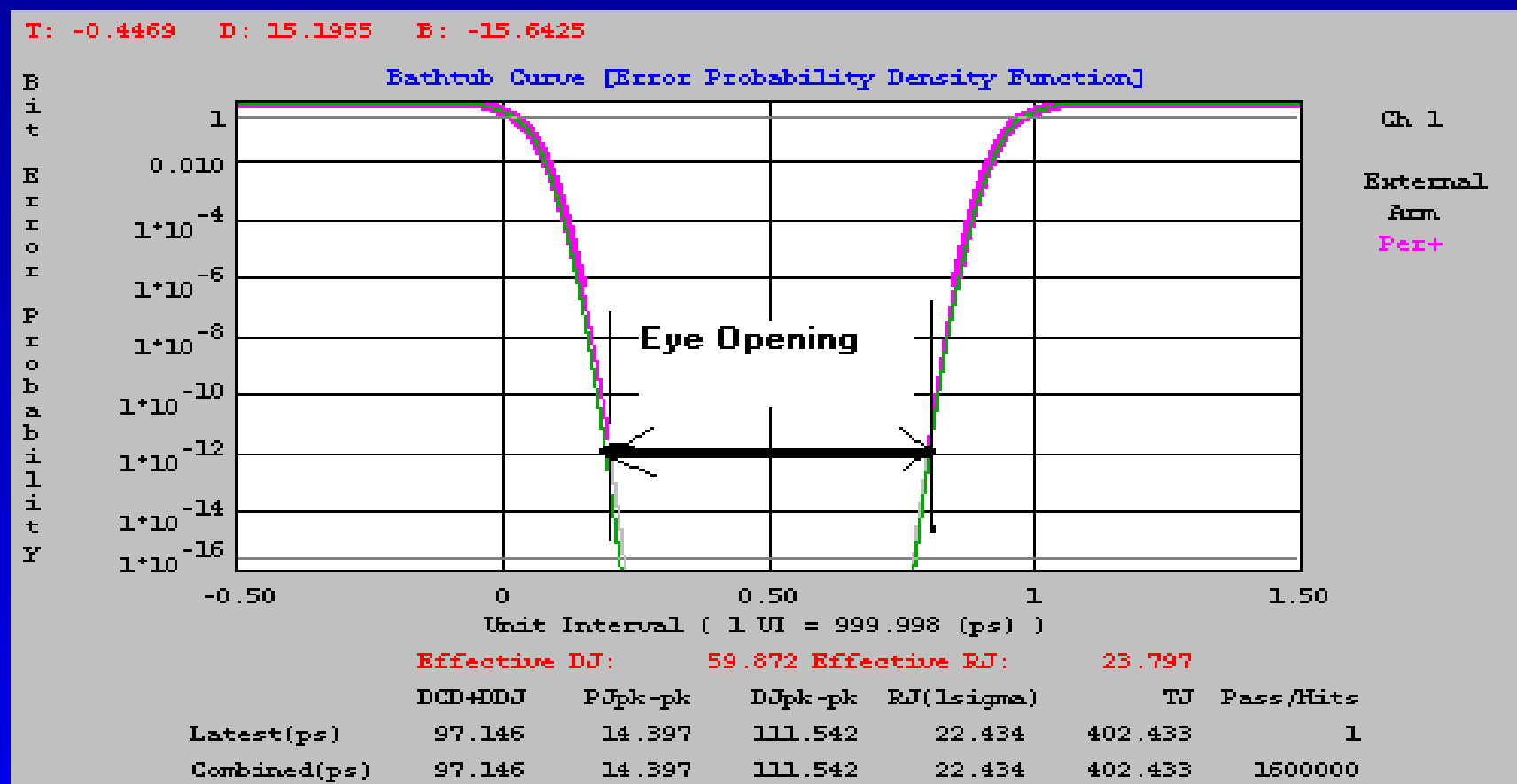


- Estimate the jitter as the receiver “sees” !!!
- CR/PLL and difference functions or their equivalents are required



Compliance Estimating/Testing: Total Jitter And BER Function

- Total jitter = UI – eye opening @ 10^{-12}



Method For Serial Links

Estimating/testing total jitter PDF via an appropriate bit clock reference

Estimating/Testing BER function to $< 10^{-12}$

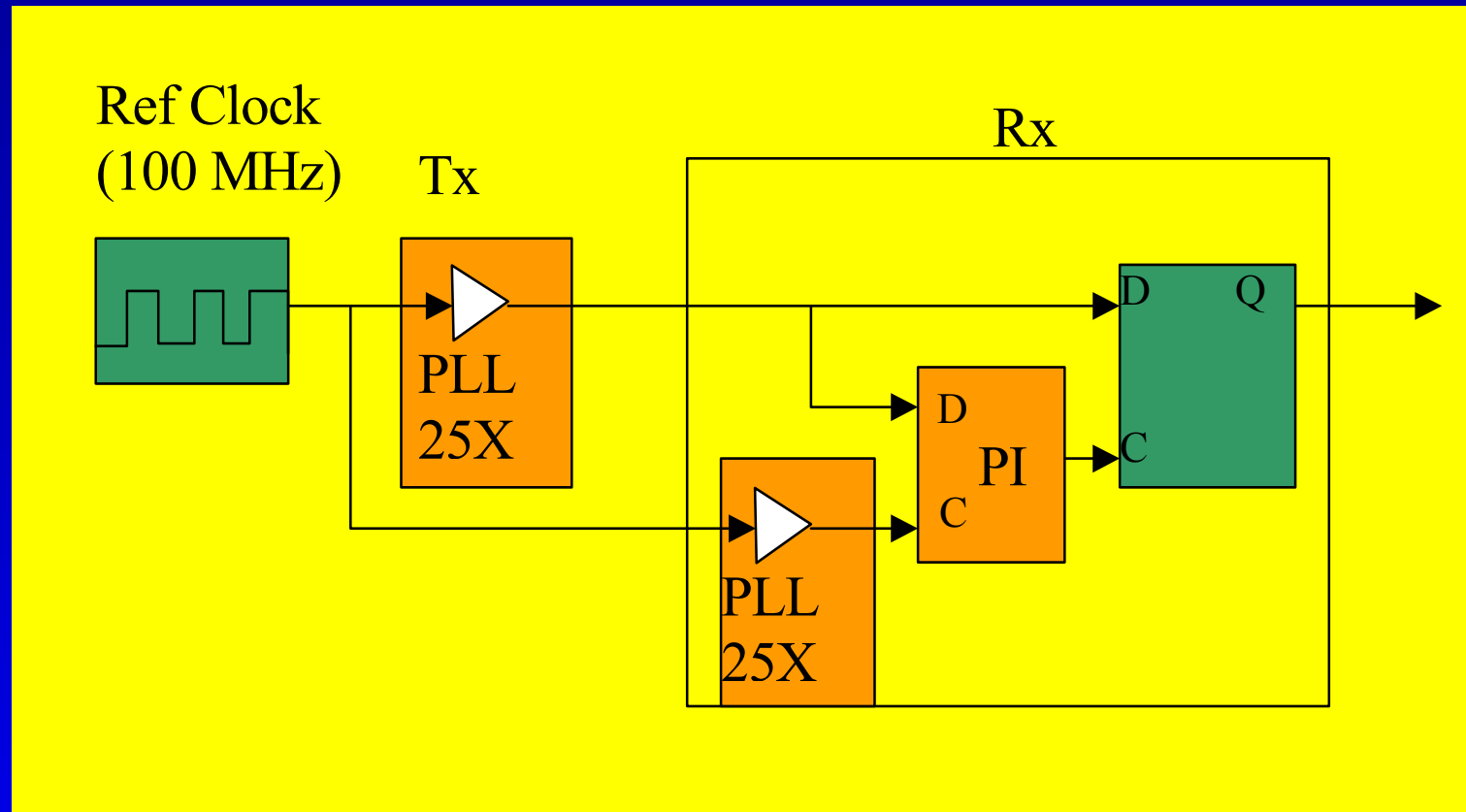
Estimating/Testing total jitter @ BER = 10^{-12} or smaller

Pass/Fail



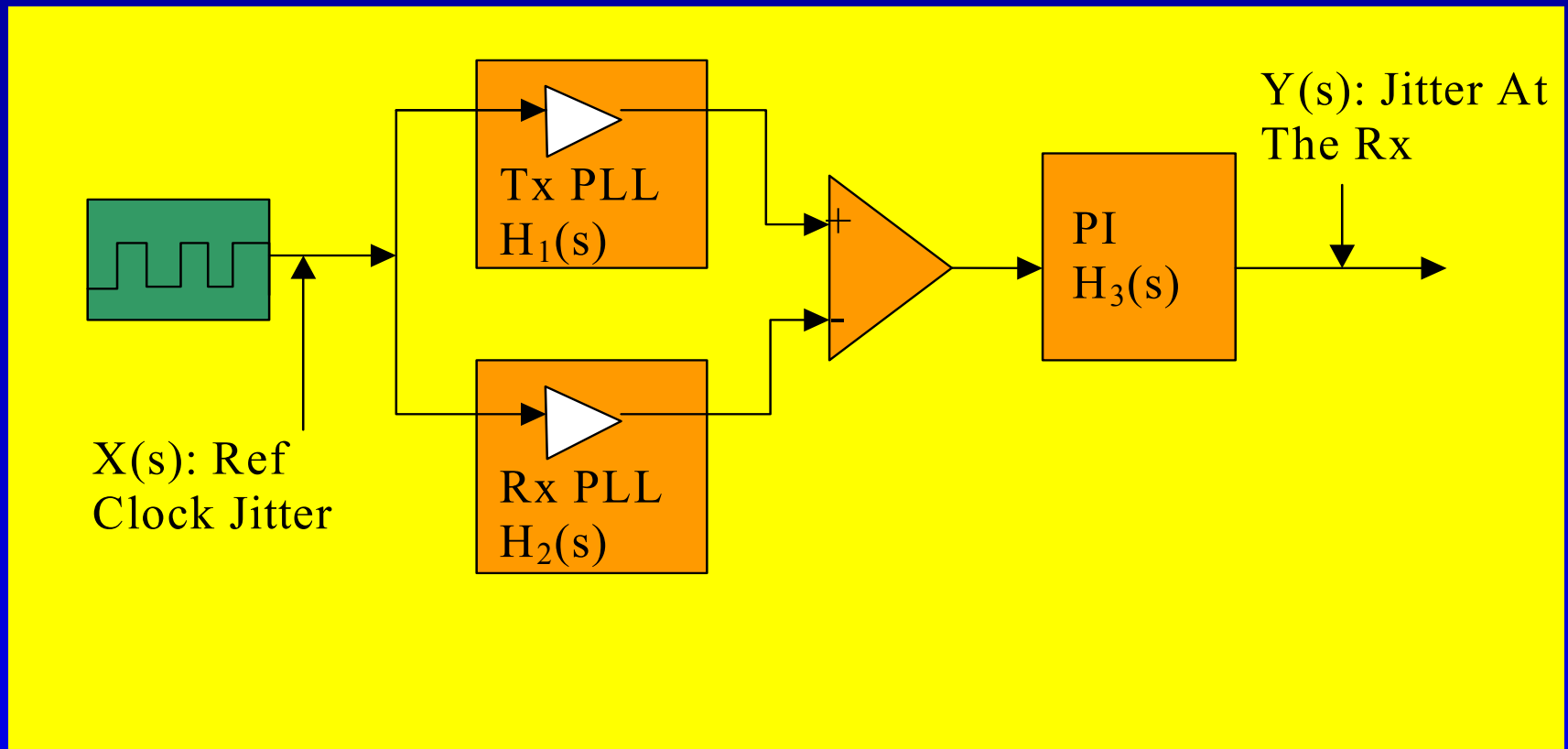
Jitter Transfer Function For PCI Express

- System block diagram for common clock mode



Jitter Transfer Function For PCI Express Cont..

- System Transfer Function Block Diagram



Jitter Transfer Function For PCI Express Cont..

- Math Relationships

$$H_t(s) = (H_1(s) - H_2(s)) \bullet H_3(s)$$

$$Y(s) = H_t(s) \bullet X(s)$$



Summary And Conclusion

- Deterministic parametric methods for jitter and noise **no longer sufficient** (e.g., Peak-to-Peak)
- **Statistical functional (PDF/CDF) methods** are required for jitter, noise, and BER estimation/test
- “Tailfit” offers deterministic and random **PDF/CDF** estimation/test
- “Autocorrelation” offers PSD for periodic and random components
- **Transfer function** is required in estimating relevant jitter, noise, and BER for the system
- **Statistical PDF/CDF + transfer function** gives a **complete and accurate** system performance estimation/testing

